

, () x - .
 . () y -
 , () t -
 .t - 25% - - 1.25t
 $\frac{x}{y}$

()	()	()	
1	$\frac{1}{x}$	x	
1	$\frac{1}{y}$	y	
$\frac{2.5t}{x}$	$\frac{2}{x}$	1.25t	2
$\frac{1.25t}{y}$	$\frac{1}{y}$	1.25t	1
$\frac{t}{x}$	$\frac{1}{x}$	t	1
$\frac{2t}{y}$	$\frac{2}{y}$	t	1

. - ,

$$\frac{2.5t}{x} + \frac{1.25t}{y} = \frac{t}{x} + \frac{2t}{y} \quad /:t > 0$$

$$\frac{2.5}{x} + \frac{1.25}{y} = \frac{1}{x} + \frac{2}{y}$$

$$\frac{1.5}{x} = \frac{0.75}{y}$$

$$\boxed{\frac{x}{y} = 2}$$

.2:1 :

2

:

$$\begin{cases} a_1 = 4 \\ a_n + a_{n+1} = 4n + 2 \end{cases}$$

, $a_{51} - a_{50}$, 100

• $(n = 50) \quad a_{50} + a_{51} = 4 \cdot 50 + 2 = 202$

. 202 :

• () -

• () $a_{n+2} - a_n$

$(n = n + 1) \quad a_{n+2} + a_{n+1} = 4 \cdot (n + 1) + 2 = 4n + 6$

$a_{n+2} + 4n + 2 - a_n = 4n + 6$

$a_{n+2} - a_n = 4$

• :

, a_{51} , 101

• - 26 -

$b_{26} = b_1 + 25d$

$b_{26} = 4 + 25 \cdot 4$

$b_{26} = 104 \rightarrow \boxed{a_{51} = 104}$

• $a_{51} = 104$:

• , - , 101

$S_{51ODD} \frac{51[2 \cdot 4 + 4(51-1)]}{2} = 5304$

$(n = 1) \quad a_1 + a_2 = 4 \cdot 1 + 2 = 6$

$4 + a_2 = 6$

$a_2 = 2$

$S_{50EVEN} \frac{50[2 \cdot 2 + 4(50-1)]}{2} = 5000$

$S_{101} = 5304 + 5000 = 10,304$

• 10,304 :

$$p(\text{man}) = \frac{2}{3}, \quad p(\text{woman}) = \frac{1}{3}$$

$$k = 2, \quad p = \frac{2}{3}, \quad n = 4$$

$$P_4(2) = \binom{4}{2} \cdot \left(\frac{2}{3}\right)^2 \cdot \left(\frac{1}{3}\right)^{4-2}$$

$$P_4(2) = \frac{4!}{2!(4-2)!} \cdot \left(\frac{2}{3}\right)^2 \cdot \left(\frac{1}{3}\right)^2$$

$$P_4(2) = 6 \cdot \left(\frac{2}{3}\right)^2 \cdot \left(\frac{1}{3}\right)^2$$

$$P_4(2) = \frac{8}{27}$$

$$\left(\frac{8}{27}\right)^2 = \frac{64}{729}$$

$$\frac{64}{729}$$

$$p(\text{Exactly 2 men} / \text{At most 2 men}) = \frac{P(\text{Exactly 2 men} \cap \text{At most 2 men})}{P(\text{At most 2 men})} = \frac{P_4(2)}{P_4(0) + P_4(1) + P_4(2)}$$

$$P_4(0) = \left(\frac{1}{3}\right)^4 = \frac{1}{81}$$

$$P_4(1) = \binom{4}{1} \cdot \left(\frac{2}{3}\right)^1 \cdot \left(1 - \frac{2}{3}\right)^{4-1}$$

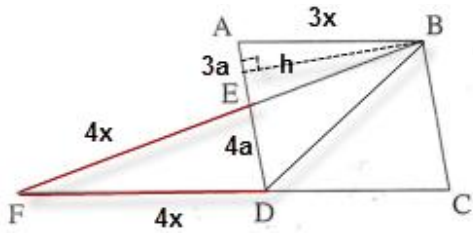
$$P_4(1) = \frac{4!}{1!(4-1)!} \cdot \left(\frac{2}{3}\right) \cdot \left(\frac{1}{3}\right)^3$$

$$P_4(1) = 4 \cdot \left(\frac{2}{3}\right) \cdot \left(\frac{1}{3}\right)^3$$

$$P_4(1) = \frac{8}{81}$$

$$p(\text{Exactl 2 men} / \text{At most 2 men}) = \frac{\frac{8}{27}}{\frac{1}{81} + \frac{8}{81} + \frac{8}{27}} = \frac{\frac{8}{27}}{\frac{11}{27}} = \frac{8}{11}$$

$$\frac{8}{11}$$



$S_{\triangle DFE} = " 48 .3 S_{\triangle ABE} = " 27 .2$

ABCD .1

BCDE .4 .

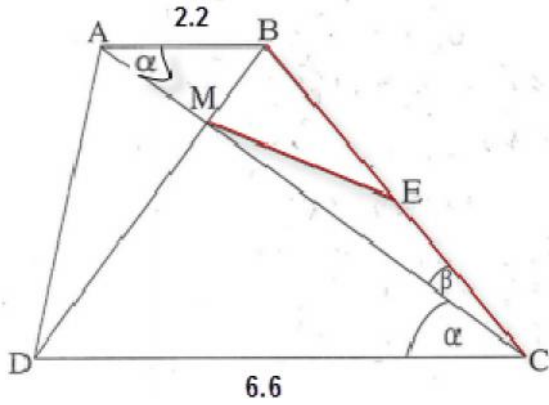
$\frac{AB}{EF} \cdot S_{\triangle BED} \cdot : "$

	ABCD	5	1
	BC AD	6	5
2	$\frac{AB}{FD} = \frac{AE}{ED} = \frac{BE}{EF}$	7	6
	$\triangle ABE \sim \triangle DFE$	8	7
	$S_{\triangle ABE} = " 27$	9	2
	$S_{\triangle DFE} = " 48$	10	3
	$\frac{S_{\triangle ABE}}{S_{\triangle DFE}} = \frac{9}{16}$	11	10, 9
	$\frac{AB}{FD} = \frac{AE}{ED} = \frac{BE}{EF} = \frac{3}{4}$	12	11, 8, 7
	$\frac{S_{\triangle ABE}}{S_{\triangle BED}} = \frac{AE \cdot h \cdot 0.5}{ED \cdot h \cdot 0.5} = \frac{3}{4}$	13	12
	$S_{\triangle BED} = " 36$	14	13, 9
. . .			
	$\sphericalangle EDF = \sphericalangle C$	15	6
	BCDE	16	4
	$\sphericalangle BED + \sphericalangle C = 180^\circ$	17	16
180°	$\sphericalangle FED + \sphericalangle BED = 180^\circ$	18	
	$\sphericalangle FED = \sphericalangle C$	19	18, 17
	$\sphericalangle FED = \sphericalangle EDF$	20	19, 15
	$\triangle EFD - EF = FD$	21	20
	$\frac{AB}{EF} = \frac{3}{4}$	22	21, 12
. . .			

.BC E , ($\sphericalangle BMC = 90^\circ$)

$\triangle BMC$.

.ME = BE = EC :



$\triangle DMC$

$$\cos \Gamma = \frac{MC}{DC}$$

$$\boxed{a \cos \Gamma = MC}$$

$\triangle MBC$

$$\cos S = \frac{MC}{BC}$$

$$\boxed{BC = \frac{a \cos \Gamma}{\cos S}}$$

$$\boxed{ME = \frac{a \cos \Gamma}{2 \cos S}}$$

.ME = $\frac{a \cos \Gamma}{2 \cos S}$:

.() $\sphericalangle BAC = \sphericalangle ACD = \Gamma$, $a = 6$, $\frac{\tan S}{\tan \Gamma} = \frac{1}{3}$.

$\triangle ABC$

$$\frac{AB}{\sin S} = \frac{BC}{\sin \Gamma}$$

$$AB = \frac{a \cos \Gamma \sin S}{\cos S \sin \Gamma}$$

$$AB = \frac{6.6 \tan S}{\tan \Gamma}$$

$$AB = \frac{6.6}{3}$$

$$\boxed{AB = 2.2}$$

.AB = " 2.2 :

. BM = " 1.3: .

2

$$\frac{AB}{DC} = \frac{BM}{MD}$$

$$MD = \frac{2.2 \cdot 1.3}{6.6}$$

$$\boxed{MD = 3.9cm}$$

ΔDMC

$$\sin r = \frac{DC}{DC} = \frac{3.9}{6.6}$$

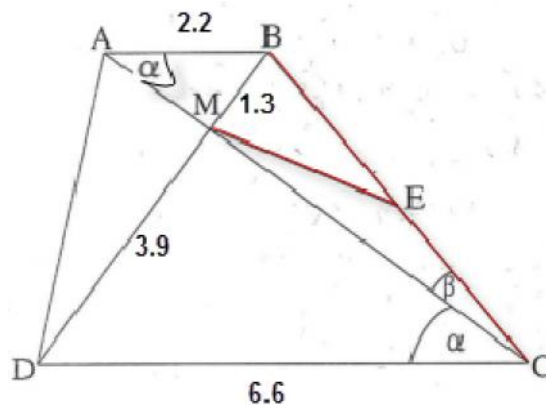
$$\boxed{r = 36.22^\circ}$$

$$\frac{\tan S}{\tan 36.22^\circ} = \frac{1}{3}$$

$$\boxed{S = 13.72^\circ}$$

$$\left. \begin{array}{l} r = 36.22^\circ \\ \frac{\tan S}{\tan 36.22^\circ} = \frac{1}{3} \end{array} \right\} \angle DCB = 36.22^\circ + 13.72^\circ = 49.94^\circ$$

. $\angle DCB = 49.94^\circ$:



• $x_A \leq x \leq x_B$, MN אורך הקטע , מקסימום

• () $0 \leq x \leq 2f$, $x -$

$$f(x) = 0.5 \sin 2x + \cos x$$

$$0.5 \sin 2x + \cos x = 0$$

$$\sin x \cos x + \cos x = 0$$

$$\cos x (\sin x + 1) = 0$$

$$\cos x = 0 \quad \sin x = -1$$

$$x = \frac{f}{2}k + f k \quad x = \frac{3f}{2}k + 2f k$$

$$x = \frac{f}{2}, \frac{3f}{2}$$

$$g(x) = \sin 2x$$

$$\sin 2x = 0$$

$$2x = f k$$

$$x = \frac{f}{2}k$$

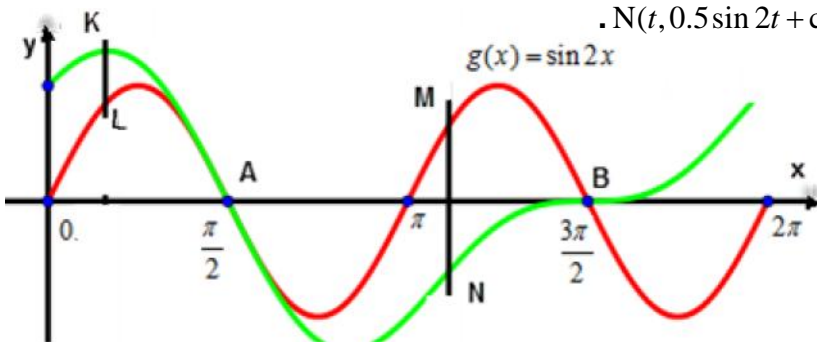
$$x = 0, \frac{f}{2}, f, \frac{3f}{2}, 2f$$

• $(A(\frac{f}{2}, 0), B(\frac{3f}{2}, 0))$ $x = \frac{f}{2}, \frac{3f}{2}$: MN

$x -$

• $(f, 0)$, $x -$,

$$g(x) \geq f(x) \quad x_A = \frac{f}{2} \leq x \leq x_B = \frac{3f}{2}$$



• $N(t, 0.5 \sin 2t + \cos t)$:

$x_N = x_M = t$ • $M(t, \sin 2t)$:

$$MN = y_M - y_N$$

$$MN = 0.5 \sin 2t - \cos t$$

$$(MN)' = \cos 2t + \sin t$$

$$1 - 2 \sin^2 t + \sin t = 0$$

$$-2 \sin^2 t + \sin t + 1 = 0$$

$$(\sin t)_1 = -0.5 \quad (\sin t)_2 = 1$$

$$\sin t = -0.5$$

$$\sin x = 1$$

$$x = -\frac{f}{6} + 2f k$$

$$x = \frac{f}{2} + 2f k$$

$$x = \frac{7f}{6} + 2f k$$

• (,) $0 \leq x \leq 2f$

$$MN(\frac{7f}{6}) = 0.5 \sin(2 \cdot \frac{7f}{6}) - \cos(\frac{7f}{6}) = \frac{3\sqrt{3}}{4}$$

$$x = \frac{7f}{6} \quad x = \frac{f}{2} :$$

$x_A = \frac{f}{2} \leq x \leq x_B = \frac{3f}{2}$, MN ,

$\frac{f}{2}$		$\frac{7f}{6}$		$\frac{3f}{2}$	x
0		$\frac{3\sqrt{3}}{4}$		0	MN(t)
Min	↖	Max	↘	Min	

$\frac{3\sqrt{3}}{4}$ MN

$0 \leq x \leq \frac{f}{2} = x_A$, **KL אורק הקטע מקסימום**

$KL(t) = -MN(t)$, $f(x) \geq g(x)$

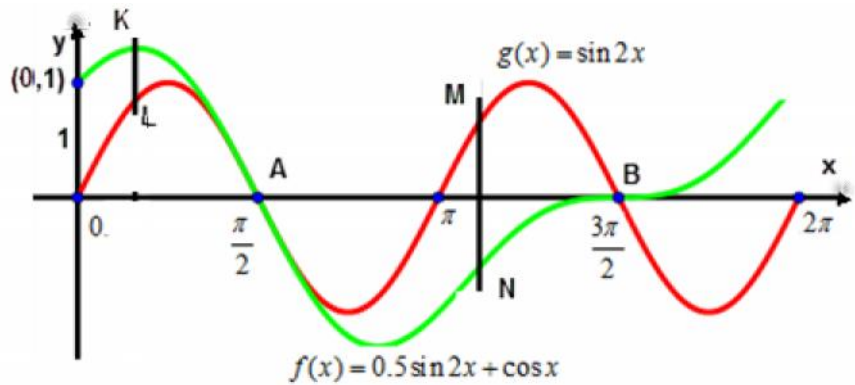
$MN(t)$, $0 \leq x \leq \frac{f}{2} = x_A$,

$KL(t)$

$KL(0) = \cos 0 - 0.5 \sin(2 \cdot 0) = 1$

$KL(\frac{f}{2}) = 0$

.1 KL :



$$g(x) = \frac{1}{\sqrt{3x^2 + 2}} \quad f(x) = \sqrt{\frac{x}{1+x^2}}$$

x , $f(x)$ (1)

$$x \geq 0$$

x x $g(x)$

$$-g(x), x \geq 0 - f(x) :$$

$$(x -) y - (2)$$

(! ,)

$$\lim_{x \rightarrow +\infty} \sqrt{\frac{x}{1+x^2}} = \lim_{x \rightarrow +\infty} \sqrt{\frac{1/x^2}{1/x^2 + 1}} = \sqrt{\frac{0}{0+1}} = 0 \rightarrow \boxed{y=0}$$

$$\lim_{x \rightarrow \pm\infty} \frac{1}{\sqrt{3x^2 + 2}} = \frac{1}{+\infty} = 0 \rightarrow \boxed{y=0}$$

$$(x \rightarrow \pm\infty)y = 0, g(x) , (x \rightarrow +\infty)y = 0 f(x) : y - :$$

$$: (3)$$

$$g(x) = \frac{1}{\sqrt{3x^2 + 2}}$$

$$g'(x) = \frac{-6x}{2\sqrt{3x^2 + 2} \cdot 3x^2 + 2}$$

$$\boxed{g'(x) = \frac{-3x}{(3x^2 + 2)^{1.5}}}$$

$$f(x) = \sqrt{\frac{x}{1+x^2}}$$

$$f'(x) = \frac{1+x^2 - 2x^2}{(1+x^2)^2} \cdot \frac{1}{2\sqrt{\frac{x}{1+x^2}}}$$

$$\boxed{f'(x) = \frac{1-x^2}{2(1+x^2)^2 \sqrt{\frac{x}{1+x^2}}}}$$

$$, x=0$$

$$(0, \frac{1}{\sqrt{2}}) :$$

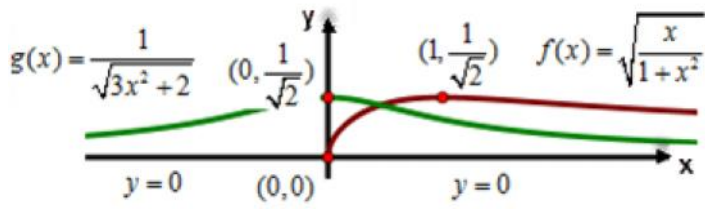
$$, x=1$$

$$(1, \frac{1}{\sqrt{2}}) , () (0,0) :$$

$$\left(\frac{1}{\sqrt{2}}\right)$$

$$.1 - 0$$

$x -$



$$.(k > 0) \quad h(x) = g(x) - k$$

$$. \quad k - , g(x)$$

$$h(x) \quad k > \frac{1}{\sqrt{2}}$$

$$f(x)$$

$x -$

$$.k > \frac{1}{\sqrt{2}} :$$

$$\cdot (k) \quad f(0) = 1, \quad f'(x) = kx + 2 : \quad \int_0^3 \left(\frac{f'(x)}{2\sqrt{f(x)}} \right) dx = 3 \quad \cdot$$

$$\int_0^3 \left(\frac{f'(x)}{2\sqrt{f(x)}} \right) dx = 3$$

$$\int_0^3 \left(\frac{1}{2\sqrt{f(x)}} \cdot f'(x) \right) dx = 3$$

$$\left[\sqrt{f(x)} \right]_0^3 = 3$$

$$\sqrt{f(3)} - \sqrt{f(0)} = 3$$

$$\sqrt{f(3)} - \sqrt{1} = 3 \quad \leftarrow f(0) = 1$$

$$\sqrt{f(3)} - 1 = 3$$

$$\sqrt{f(3)} = 4$$

$$\boxed{f(3) = 16}$$

$$f'(x)$$

$$, f'(x) = kx + 2$$

$$f(x) = \int f'(x) dx$$

$$f(x) = \int (kx + 2) dx$$

$$f(x) = \frac{kx^2}{2} + 2x + c$$

$$1 = \frac{k \cdot 0^2}{2} + 2 \cdot 0 + c \quad \leftarrow f(0) = 1$$

$$\boxed{c = 1}$$

$$16 = \frac{k \cdot 3^2}{2} + 2 \cdot 3 + 1 \quad \leftarrow f(3) = 16$$

$$\boxed{k = 2}$$

$$\boxed{f(x) = x^2 + 2x + 1 = (x+1)^2}$$

$$\cdot f(x) = x^2 + 2x + 1 = (x+1)^2, \quad f(3) = 16 : \quad \cdot$$

$$g(x) = \sqrt{f(x)} \quad (1)$$

$$g(x) = |x+1| \quad g(x) = \sqrt{(x+1)^2}$$

$$g(x) = \begin{cases} x+1 & x \geq -1 \\ -x-1 & x < -1 \end{cases}$$

$$g(x) = |x+1|$$

$$g(x) = f(x) = 1 \quad (2)$$

$$\sqrt{f(x)} = f(x) = 0 \quad (-1,0) \quad \sqrt{f(x)} = f(x) = 1$$

